# An Empirical Evaluation of Mutation and Crossover Operators for Multi-Objective Uncertainty-Wise Test Minimization

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Abstract—Multi-objective uncertainty-wise test case minimization focuses on selecting a minimum number of test cases to execute out of all available ones while maximizing effectiveness (e.g., coverage), minimizing cost (e.g., time to execute test cases), and at the same time optimizing uncertaintyrelated objectives. In our previous unpublished work<sup>1</sup>, we developed four uncertainty-wise test case minimization strategies relying on Uncertainty Theory and multi-objective search (NSGA-II with default settings), which were evaluated with one real Cyber-Physical System (CPS) with inherent uncertainty. However, a fundamental question to answer is whether these default settings of NSGA-II are good enough to provide optimized solutions. In this direction, we report one of the preliminary empirical evaluations, where we performed an experiment with three different mutation operators and three crossover operators, i.e., in total nine combinations with NSGA-II for the four uncertainty-wise test case minimization strategies using a real CPS case study. Results show that the Blend Alpha crossover operator together with the polynomial mutation operator permits NSGA-II achieving the best performance for solving our uncertainty-wise test minimization problems.

## Keywords—Uncertainty-Wise Testing; Test Case Minimization; Multi-objective Search; Cyber-Physical Systems

### I. INTRODUCTION

The internal behavior of a Cyber-Physical System (CPS) under Test (CUT) is typically known to a limited extent [1-3]. In addition, a CPS interacts with the physical environment including agents (e.g., human), which is fundamentally indeterminate [1-3]. This means that uncertainty regarding the internal behavior of a CUT must be explicitly taken into the account together with uncertainty in its environment when performing any kind of testing. Traditional testing methods for CPS [4-6] do not handle uncertainty explicitly and thus novel testing approaches for CPS must be made "uncertainty-wise".

In the direction of making testing techniques "uncertaintywise", we proposed an uncertainty testing framework called UncerTest in our previous unpublished work <sup>1</sup> [7]. The UncerTest framework defines a set of uncertainty-wise test case generation and minimization strategies for CPSs. The key inputs for UncerTest are tested ready models of a CUT with explicitly modeled subjective uncertainty on its internal behavior and test ready models of the physical environment with uncertainty. Such test ready models (extended UML class diagram, state machines, and object diagrams) were developed with our uncertainty modeling framework called UncerTum presented in [8]. Uncertainty-wise test case minimization strategies in UncerTest were designed and implemented based on Uncertainty Theory [9] and multi-objective search (NSGA-II [10] with default settings) and were evaluated with a real CPS in terms of their cost, effectiveness, and efficiency.

Uncertainty-wise test case minimization strategies take into consideration cost and effectiveness measures, including a number of test cases to execute (cost), high coverage (transition coverage), and at the same time focused on optimizing uncertainty-related objectives [7]. These uncertainty related objectives are a number of uncertainties in a test case, the number of unique uncertainties in a test case, uncertainty space coverage and uncertainty measure of a test case defined with the uncertainty theory [9].

Our initial evaluation of the above mentioned uncertaintywise test case minimization strategies [7] only experimented with default settings of NSGA-II implemented in jMetal [11]. A fundamental question to answer is whether these default settings of NSGA-II are good enough for uncertainty-wise test case minimization strategies. To this end, we report a preliminary empirical evaluation, where we compared nine combinations of mutation and crossover operators (three crossover and three mutation operators) with NSGA-II, using a CPS case study for the four uncertainty-wise test case minimization strategies reported in [7]. The case study is a real CPS about GeoSports provided to us by Future Position X, Sweden (FPX)<sup>2</sup> as part of our on-going project [12] with FPX as an industrial partner.

Results of our empirical evaluation show that the Blend Alpha crossover (BLX- $\alpha$ ) operator together with the polynomial mutation operator can assist NSGA-II to attain the best performance for our four uncertainty-wise test

<sup>&</sup>lt;sup>1</sup> This is an unpublished work (reference number [7]) reported in a project deliverable and made available as a technical report.

<sup>&</sup>lt;sup>2</sup> www.fpx.se

minimization problems, corresponding to the four uncertaintywise test strategies. Moreover, we observed that regardless of the chosen mutation operator, the BLX- $\alpha$  crossover operator performs significantly better than the rest of the studied crossover operators.

This paper is organized as follows: Section II presents the background to understand the remaining sections of the paper. Section III presents the planning of our empirical evaluation. Section IV provides results and analyses. Section V presents the related work and we conclude the paper in Section IV.

# II. BACKGROUND

In a project deliverable<sup>1</sup> [7], we presented UncerTest, an uncertainty-wise test case generation, and minimization framework. The input of UncerTest is test ready models explicitly capturing uncertainty developed with UncerTum an uncertainty-wise test modeling framework<sup>3</sup> [8]. With UncerTum test ready models are created with UML state machines, UML class diagrams, and UML object diagrams. Uncertainty information is added to various model elements using the UML Uncertainty Profile (UUP) defined in UncerTum. The UML state machines with applied UUP are called Belief State Machines (BSMs). UncerTest then utilizes two implemented test case generation strategies and four minimization test strategies relying on the uncertainty theory [9] and multi-objective search to generate executable test cases. Such test cases are executed on a CPS to test its implementation in the presence of uncertainty.

In UncerTest (reported in a project deliverable<sup>1</sup>) [7], we defined four test case minimization problems that were solved with multi-objective search. These problems with their minimization objectives are listed in TABLE I.

TABLE I. UNCERTAINTY-WISE TEST CASE MINIMIZATION PROBLEMS [7]

<b>P</b> #	↓Objective 1	↑ Objective 2	↑ Objective 3
D1		Average # of Uncertainties	
ГІ		covered	
P2	% of test case	% Uncertainty Space	%Transition
12	70 OI test case	coverage	coverage
P3	minimization	Average Uncertainty Measure	-
D/		% Unique Uncertainties	
14		covered	

Each test case has the following associated attributes: 1) number of subjective uncertainties covered (Objective 2 for P1), 2) uncertainty space covered as defined in the uncertainty theory (Objective 2 for P2), 3) overall uncertainty of a test case calculated using the uncertainty measure defined in the uncertainty theory (Objective 2 for P3), 3) number of unique uncertainties covered (Objective 2 for P4), and 4) number of transitions covered (Objective 3 for P1--P4).

A test case minimization solution consists of a subset  $(T_{msub})$  of a total number of test cases  $(T_{total})$ .  $T_{total}$  is generated

from a BSM, i.e., a test ready model using a test case generation strategy implemented in UncerTest.

Objective 1 is calculated as:  $01 = \frac{T_{msub}}{T_{total}} \times 100\%$ .

Objective 2 for P1 (i.e., Average # of Uncertainties covered) is calculated as follows:

$$O2_{P1} = \frac{\sum_{i=1}^{NT_{\text{msub}}} nor(NU(t_i'))}{NT_{\text{msub}}}$$

In the above formula,  $NT_{\text{msub}}$  is the number of test cases in the minimized subset. NU represents the number of uncertainties in a test case and  $nor(NU(t_i')) = \frac{NU(t_i')}{NU(t_i') + 1}$ [13].

Objective 2 for P2 (i.e., % Uncertainty Space coverage) is calculated as follows:

$$O2_{P2} = \frac{musp}{nusp} \times 100\%$$

In the above formula, *nusp* represents the uncertainty space covered [9] by a BSM from which the test cases are generated, whereas *musp* represents the uncertainty space of  $T_{msub}$ .

Objective 2 for P3 (i.e., Average Uncertainty Measure) is calculated as follows:

$$O2_{P3} = \frac{\sum_{i=1}^{NT_{\text{msub}}} UM(t_i)}{NT_{\text{msub}}}$$

In the above formula,  $NT_{msub}$  is the number of test cases in the minimized subset. UM(t<sub>x</sub>) represents the uncertainty measure of a test case x using the uncertainty theory [9].

Objective 2 for P4 (i.e., Unique Uncertainties Covered) is calculated as follows:

$$O2_{P4} = \frac{muu}{nuu} \times 100\%$$

In the above formula, *muu* is the number of unique (nonduplicate) uncertainties covered by  $T_{msub}$ , whereas *nuu* is the total number of uncertainties in a BSM.

Objective 3 is calculated as:  $03 = \frac{mtr}{ntr} \times 100\%$ .

In the above formula, mtr is the number of unique transitions covered by  $T_{msub}$ , whereas ntr is the total number of transitions in the BSM.

In the project deliverable (unpublished work) [7], we used NSGA-II, the commonly used multi-objective search algorithm to solve these four test case minimization problems. We used the NSGA-II algorithm implemented in jMetal [11] with the default parameter settings.

## III. EMPIRICAL EVALUATION PLANNING

In this section, we will present our overall objective and research questions (Section A), selection of the case study, the algorithm, and operators (Section B), and design of our experiment in Section C.

<sup>&</sup>lt;sup>3</sup> Notice that [8] is a technical report (under review of Sosym journal) reporting a project deliverable.

TABLE II. DESIGN OF THE EXPERIMENT\*

A. Overall Objective and Research Questions

Our overall objective is to study the impact of various mutation and crossover operators for NSGA-II on the effectiveness of the four uncertainty-wise test case minimization techniques described in Section II and were originally proposed in [7]. Based on our overall objective, we defined the following research questions:

**RQ1:** For each uncertainty-wise test case minimization strategy (P1 to P4 in Section II), how does NSGA-II compare with the Random Search (RS), with each combination of the mutation and crossover operator?

**RQ2:** Which combination of the mutation and crossover operator helps an uncertainty-wise test case minimization strategy (P1 to P4 in Section II) in achieving the best performance?

**RQ3:** How do the interactions among the crossover and mutation operators affect the performance of uncertainty-wise test case minimization strategies?

The first research question helps us in assessing whether the problems we are solving are complex and deserve the use of a complex multi-objective search algorithm. Notice that this is according to the commonly used guidelines for applying search-based algorithms in software engineering [14]. The second research question helps us in determining one or more best combinations of the mutation and crossover operators that we can recommend to use with each uncertainty-wise test case minimization strategy. The third research question helps us in studying the interactions among crossover and mutation operators on the performance of NSGA-II.

# B. Selection of Case Studies, Algorithm, and Operators

In this section, we present the two case studies that we selected for our empirical evaluation, in addition to the selection of the mutation and crossover operators.

# 1) Case Study

The case study is provided by Future Position X (FPX), Sweden<sup>2</sup>—one of the industrial partners in our on-going project [12]. The case study is an instance of GeoSports for Bandy (a type of ice hockey). The CPS involves attaching various sensors to collect health and bandy related measurements including heartbeat, speed, and location. The collected measurements are then transferred at runtime via a receiver station (a Bluetooth-based antenna) to a computer system, where those measurements can be monitored by Bandy coaches. To facilitate automated execution of tests on such CPS without real players, Nordic Med Test (NMT)<sup>4</sup>—another partner provides test execution infrastructure. Given that the physical infrastructure is used for execution of tests, maximizing the effectiveness of test case execution with a minimum number of test cases is of utmost importance due to the fact that it is expensive both in terms of time to set up, execute, and maintain it.

For the Bandy case study, we used UncerTum [8] to create test ready models as reported in [7] and UncerTest with *All Path with Maximum Length (APML)* was used to generate test cases [7]. In total, for Bandy, 2085 test cases were generated. These test cases were the input for our uncertainty-wise test case minimization. Notice that for each test case, a number of uncertainties, uncertainty space coverage, uncertainty measure, and the number of unique uncertainties were calculated automatically. Notice that in Section II, we briefly explained these attributes; however further details can be consulted in [7].

# 2) NSGA-II Settings and Operators

We selected three mutation operators and three crossover operators for NSGA-II—the most commonly used algorithm for multi-objective optimization. The crossover operators include Simulated Binary Crossover (SBX), Single Point Crossover (SPX), and Blend Alpha Crossover (BLX- $\alpha$ ) [15]. The mutation operators include Polynomial (M1), Non-Uniform (M2), and Swap (M3). Thus, we had nine combinations of the mutation and crossover operators (CM<sub>1</sub> to CM<sub>9</sub>).

Given that random variation is inherent in search algorithms, we ran NSGA-II and RS 100 times each to deal with the random variation. We used the jMetal framework [11] for the implementation of both NSGA-II and RS. The population size was set to 100, the binary tournament was used for the selection parents, and the simulated binary criterion was used for recombination. Notice that as an initial empirical evaluation, we only evaluated the combination of the mutation and crossover operators and kept the rest of the settings default.

# C. Experiment Design

The design of our experiment is shown in TABLE II. As shown in the table, for each uncertainty-wise test case minimization problem (P1--P4) as described in Section II, we used the Bandy case study to answer the three research questions defined in Section A.

For RQ1 as shown in TABLE II, we compared NSGA-II together with each combination of the crossover and mutation

<sup>4</sup> www.nordicmedtest.se/

operators (CM<sub>1</sub> to CM<sub>9</sub>) with RS, i.e., in total 9 comparisons. For RQ2, we compared NSGA-II with each pair of the combinations of the crossover and mutation operators, for example, NSGA-II (with CM<sub>1</sub>) with NSGA-II (with CM<sub>2</sub>) and so on. In total, we have  ${}^{9}C_{2}$  pairs of comparisons. For RQ3, we performed interaction analysis of the crossover and mutation operators on the performance of NSGA-II.

As shown in the Metrics column of TABLE II, for each pair of comparison, we used a set of metrics. First, we used HyperVolume (HV) [16] as the quality indicator, which was selected based on the guidelines of selecting an appropriate quality indicator for search-based software engineering (SBSE) problems [17]. Second, we also performed the comparison using the individual objectives relevant for each problem, i.e., O1, O2<sub>P1</sub>, O3 for P1, O1, O2<sub>P2</sub>, O3 for P2, O1, O2<sub>P3</sub>, O3 for P3, and O1, O2<sub>P4</sub>, O3 for P4. Notice that in each run of NSGA-II, it produces a set of non-dominated solutions (100 in our case) constituting a Pareto front. For each individual objective (e.g., O1), we select the best solution with the highest value of the objective function (e.g., O1) for comparison out of all the 100 non-dominated solutions produced by NSGA-II in this run. Third, we also performed the comparison using Overall Fitness Value (OFV) for each problem (P1--P4). OFV<sub>P1</sub> is calculated as (O1+O2<sub>P1</sub>+O3)/3, OFV<sub>P2</sub> is calculated as (O1+O2<sub>P2</sub>+O3)/3, OFV<sub>P3</sub> is calculated as (O1+O2<sub>P3</sub>+O3)/3, and OFV<sub>P4</sub> is calculated as  $(O1+O2_{P4}+O3)/3$ . For each run, we calculate OFV for each of the 100 non-dominated solutions for each run. In this way, we have 100\*100 (10,000) OFV values to compare for 100 runs.

In terms of statistical methods, for each pair of comparison, we used  $\widehat{A_{12}}$  as an effect size measure, whereas the Mann-Whitney U Test was used to assess the statistical significance of results. These two tests were chosen based on the guidelines of reporting results of SBSE [14]. For RQ2, since we have ( ${}^{9}C_{2}$ ), i.e., 36 pair-wise comparisons, we first used the Kruskal– Wallis test with Bonferroni Correction to determine if overall statistically significant differences exist among all the pairs together. For both the Mann-Whitney and Kruskal–Wallis, we chose the significance level of 0.05, i.e., a value less than 0.05 shows statistically significant differences. In case of significant differences, pair-wise comparisons were performed with the Mann-Whitney U Test. In terms of  $\widehat{A_{12}}$ , a value of 0.5 means no difference between a pair being compared, a value less than 0.05 means that the first in the pair has higher chance to get a better solution than the second one, whereas a value greater than 0.5 means vice versa. For RQ3, we chose the Two-Way Analysis of Variance (ANOVA) to study the interactions among the crossover and mutation operators on objective values and HV [18, 19].

### IV. RESULTS AND ANALYSIS

In this section, we present our results and analyses corresponding to the research questions.

## A. Results for RQ1

All the detailed results are provided in Appendix A. For P1 in terms of O1,  $O2_{P1}$ ,  $OFV_{P1}$ , and HV, NSGA-II performed significantly better than RS. For O3, either there were no significant differences between NSGA-II and RS or RS was significantly better than NSGA-II. Recall that O3 is about the *All Transition* coverage and thus RS always selected more test cases (i.e., less percentage of test minimization) and thus covered more transitions than NSGA-II. For P2, P3, and P4, we observed the similar pattern as P1, except that for O3, we didn't observe any difference between NSGA-II and RS.

Based on the results, we can conclude that regardless of the combination of the mutation and crossover operators, NSGA-II managed to significantly outperform RS in terms of HV and OFV, suggesting that our problems are difficult to solve and require the use of multi-objective search algorithms.

#### B. Results for RQ2

To answer RQ2, for each problem (P1--P4), first, we compared overall differences among ( ${}^{9}C_{2}$ ), i.e., 36 combinations all together using the Kruskal–Wallis test with Bonferroni Correction and results are summarized in TABLE OF EACH PROFILEM FOR EACH OPDECTIVE

Problems	Metrics	Rank1	Rank2	Rank3	Rank4	Rank5	Rank6	Rank7	Rank8	Rank9
	01	CM <sub>7</sub>	CM <sub>8</sub>	CM <sub>9</sub>	$CM_1$	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>5</sub>	CM <sub>6</sub>
	$O2_{P1}$	CM <sub>7</sub>	CM <sub>8</sub>	CM <sub>9</sub>	CM <sub>1</sub>	$CM_2$	CM <sub>3</sub>	$CM_4$	CM <sub>5</sub>	CM <sub>6</sub>
P1	03	(C	$M_2 = CM_5 =$	CM <sub>6</sub> )	(CN	(CM <sub>1</sub> =CM <sub>3</sub> =CM		CM <sub>8</sub>	(CM <sub>7</sub> :	=CM9)
	$OFV_{P1}$	$(CM_7=CM_8)$		CM <sub>9</sub>	CM <sub>1</sub>	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>5</sub>	$CM_6$
	HV	CM <sub>7</sub>	(CM	[8=CM9)	CM <sub>1</sub>	(CM2=	=CM <sub>3</sub> )	$CM_4$	(CM5	=CM <sub>6</sub> )
	01	(CM <sub>7</sub> =	$=CM_8)$	CM <sub>9</sub>	$CM_1$	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
P2	O2 <sub>P2</sub>	-	-	-	-	-	-	-	-	-
	03	-	-	-	-	-	-	-	-	-
	OFV <sub>P2</sub>	$(CM_7=CM_8)$		CM <sub>9</sub>	$CM_1$	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
	HV	(CM7=CM8=CM9)			CM <sub>1</sub>	(CM <sub>2</sub> =	=CM <sub>3</sub> )	$CM_4$	(CM5	$=CM_6)$
	01	(C	$M_7 = CM_8 =$	CM <sub>9</sub> )	CM <sub>1</sub>	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
	O2 <sub>P3</sub>	(C	$M_7 = CM_8 =$	CM <sub>9</sub> )	CM <sub>1</sub>	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
P3	O3	-	-	-	-	-	-	-	-	-
	OFV <sub>P3</sub>	(C	$M_7 = CM_8 =$	CM <sub>9</sub> )	CM <sub>1</sub>	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
	HV	CM7=C	$CM_9$	CM <sub>8</sub> =CM <sub>9</sub>	CM <sub>1</sub>	CM <sub>3</sub>	$CM_2$	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
	01	CM <sub>9</sub>	CM <sub>7</sub>	CM <sub>8</sub>	CM <sub>1</sub>	$CM_2$	CM <sub>3</sub>	$CM_4$	CM <sub>5</sub>	CM <sub>6</sub>
	$O2_{P4}$	-	-	-	-	-	-	-	-	-
P4	O3	-	-	-	-	-	-	-	-	-
	OFV <sub>P4</sub>	CM <sub>9</sub>	CM <sub>7</sub>	CM <sub>8</sub>	CM <sub>1</sub>	$CM_2$	CM <sub>3</sub>	$CM_4$	CM <sub>6</sub>	CM <sub>5</sub>
	HV	(C	$M_7 = CM_8 =$	CM <sub>9</sub> )	$CM_1$	(CM <sub>2</sub> =	$=CM_3)$	$CM_4$	(CM <sub>5</sub> =	$=CM_6)$

TABLE III. RANKS OF THE COMBINATIONS FOR EACH PROBLEM FOR EACH OBJECTIVE

IV. Notice that most of the time, p-values are less than 0.0001 suggesting that significant differences exist among pairs in terms of the individual objectives, OFV, and HV. For the cells with a "-" value means no significant differences. We further compared each pair of crossover and mutation operator using the Mann-Whitney U Test and  $A_{12}$ , only for the cases when the Kruskal–Wallis test revealed significant differences. Due to the large number of comparisons and lack of space in this paper, we only report summarized results in TABLE IV. However, the detailed results including p-values and  $A_{12}$  are reported in Appendix B.

TABLE IV. RESULTS OF THE KRUSKAL-WALLIS TEST

Problems	01	$O2_{Pi}$ for Pi	03	OFV <sub>Pi</sub> for Pi	HV
P1	<.0001	<.0001	<.0001	<.0001	<.0001
P2	<.0001	-	-	<.0001	<.0001
P3	<.0001	<.0001	-	<.0001	<.0001
P4	<.0001	-	-	<.0001	<.0001

In TABLE III, a "-" means that we did not perform a pairwise comparison since we did not observe overall differences using the Kruskal–Wallis test (e.g.,  $O2_{P2}$  and O3 for P2). For P1, except for O3, CM<sub>7</sub> is the best combination. For P2, CM<sub>7</sub> and CM<sub>8</sub> are the best combinations for O1 and OFV<sub>P2</sub> and for HV CM<sub>7</sub> to CM<sub>9</sub>. For P3, O1, O2<sub>P3</sub>, OFV<sub>P3</sub>, CM<sub>7</sub> to CM<sub>9</sub> are the best combinations, whereas for HV both CM<sub>7</sub> and CM<sub>9</sub> are the best ones. For P4, when looking at O1 and  $OFV_{P1}$ ,  $CM_9$  is the best, whereas for HV  $CM_7$  to  $CM_9$  are the best combinations.

Across all the problems, when we consider HV—the most commonly used quality indicator used to assess the quality of solutions produced by Pareto optimality based algorithms [16, 17], we have a clear winner, i.e.,  $CM_7$ . The  $CM_7$  is the combination of the BLX- $\alpha$  crossover operator with the polynomial mutation operator.

### C. Results for RQ3

For each problem, we additionally performed Two-Way ANOVA to study the significance of the interactions among the crossover and mutation operators on the objectives and HV. The detailed results with exact p-values are provided in Appendix C. We only provide interaction plots for all the four problems, only for those objectives/HV when the interactions had a significant impact on objectives/HV. For example, for P1, there were no significant interactions for O2<sub>P1</sub> and O3 and for the rest, the results were significant (p<0.05) and thus we do not show plots for O2<sub>P1</sub> and O3. In Figure 1 for P1, in terms of O1/O2<sub>P1</sub>/OFV<sub>P1</sub>, C1 and C3 give the best results with M1 and M2 (lower values), whereas when considering mutation operators (M1-M3), C3 has the best performance with all the



mutation operators followed by C1 and C2. For HV (notice that higher values mean better performance), the results are also consistent. For P2/P4, the observed results are exactly the same as P1. For P3, results are the same as well except that we had additional results for  $O2_{P3}$ , which are also consistent with the rest of the objectives.

Based on the above results, we can conclude that the C3 crossover mutation operator with any mutation operator consistently gives the best results for all the four uncertainty-wise test minimization problems.

# D. Overall Discussion

Based on the results and discussions in the previous sections, we recommend using  $CM_7$  together with NSGA-II with default parameter settings to solve our uncertainty-wise test case minimization problems. Since  $CM_7$  (equal to  $CM_8$  or equal to  $CM_9$ ) turns out to be the winner, when considering HV, i.e., the most commonly used quality indicator to assess the quality of the solutions produced by multi-objective search algorithms based on the Pareto optimality theory.

When further analyzing CM<sub>7</sub> to CM<sub>9</sub>, we can see that all the three combinations use the same crossover operator, i.e., BLX- $\alpha$  and it gives us an indication that this crossover operator plays a significant role on the performance of NSGA-II for our uncertainty-wise test case minimization problems. This was further confirmed with the interactions analyses reported in Section C, where C3 (i.e., the BLX- $\alpha$  operator) with any combination of the mutation operator was the best one for all the four problems (Figure 1).

Evidence has shown that BLX- $\alpha$  has a good capability of exploring a search space [20, 21], as compared to, for example, SBX and SPX. One probable explanation is that in our context, NSGA-II needed to explore more search space (in a given number of generations) as compared to exploiting the nearby search space of parents, to find the most optimized solutions. However, this explanation needs to be further justified with further experimentation and theoretical analysis that we plan to conduct in the near future.

#### E. Threats to Validity

All the experiments have their associated threats to validity. In terms of *internal validity*, we used default parameter settings of *NSGA-II* except for the combinations of crossover and mutation operators. However, these default values were chosen based on the guidelines reported in [14, 22, 23]. Additionally, in this preliminary experiment, we only chose three crossover and three mutation operators, and several other such operators exist that can be used. We chose these operators since their implementation was readily available in jMetal. We plan to conduct more experiments in the near future to include more crossover and mutation operators. In terms of *external validity* threats, we only used one industrial case study and no doubt, additional experiments with different case studies are necessary to generalize the results.

For *conclusion validity* related to the randomness of solutions produced by search algorithms [24], we repeated the

experiments 100 times [24] according to standard guidelines [14]. Following the same guidelines, we used the appropriate statistical tests, e.g., the Vargha and Delaney statistics to calculate effect size, and the Mann-Whitney U test to determine the significance of results. *Construct validity* threats are concerned with the use of measures for comparing performance [24]. We used the same stopping criterion (25000 fitness evaluations [24]) for all NSGA-II and RS to avoid any potential bias in results.

## V. RELATED WORK

A detailed survey on SBSE is reported in [25]. The survey reports various types of software engineering problems that are solved with SBSE in addition to reporting various trends of search algorithms' applications and techniques. Based on the review, it is clear that test case minimization is one of the widely addressed problems in SBSE. Other surveys reported in [26] and [27], provide various test optimization objectives in the context of regression testing, e.g., based on code coverage and fault detection. In addition, even existing search-based test optimization approaches are based on typical cost measures, e.g., time to execute test cases and measure effectiveness, for instance, using code coverage [28, 29] and fault detection [17, 30, 31]. Our uncertainty-wise test case minimization objectives, i.e., the number of uncertainties, the number of unique uncertainties, uncertainty space coverage, and uncertainty measure are new. However, transition coverage has been already been studied [27, 32].

Our uncertainty testing framework, named as UncerTest was reported in the project deliverable<sup>1</sup> [7], where we originally proposed uncertainty-wise test case generation and minimization approaches. However, in [7], we only experimented with the default parameter settings and default mutation and crossover operators of NSGA-II. In this work, we experimented with combinations of the mutation and crossover operators. Based on the results of our experiments, the guidelines for selecting an appropriate combination of the mutation and crossover operator are proposed. These guidelines will be implemented in UncerTest.

In our another work reported in [33], we proposed an uncertainty-wise time-aware test prioritization approach that uses the same objectives as this one but focuses exclusively on test prioritization rather than minimization as the project deliverable reported in [7] and in this paper. In addition, the key contribution of this paper is to empirically investigate various combinations of the mutation and crossover operators with NSGA-II with the ultimate aim of deriving a set of guidelines to select an appropriate combination of the mutation and crossover operators for our problems.

Existing search-based optimization approaches address uncertainty in software project planning [34] and in the early stage, e.g. requirement analysis [35-37] to enable the decision making in uncertainty. In contrast, our works [7, 33] address uncertainty in test optimization.

# VI. CONCLUSION AND FUTURE WORK

This paper presented an empirical evaluation assessing the effect of 9 combinations of 3 crossover and 3 mutation operators on the performance of NSGA-II for four uncertaintywise test case minimization problems. We used test cases generated for a real Cyber-Physical System (CPS) provided by Future Position X related to GeoSports (for Bandy sports). The results of the empirical evaluation show that the Blend Alpha Crossover operator (BLX- $\alpha$ ) with the polynomial mutation operator enables NSGA-II to achieve the best performance for our uncertainty-wise test case minimization problems. Furthermore, we concluded that for our problems, BLX- $\alpha$  with other evaluated mutation operators also gave good performance suggesting that irrespective of a mutation operator, BLX- $\alpha$  can help NSGA-II achieve the best performance for our uncertainty-wise test case minimization problems. In the future, we would like to extensively extend our empirical evaluation with additional mutation and crossover operators and include other case studies for evaluation.

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# Appendix A. Statistic Analysis Result for RQ1

Table A 1. Mann-Whitney U	J Test between NSGA-II (C	CM1-CM9) VS RS Fo	r P1 with Bandy
rubic if it it it in the second of the secon		(111  only)	I I I with Dunay

	CM			Metrics		
Prob	CM	01	O2 <sub>Pi</sub> for Pi	03	OFV <sub>Pi</sub> for Pi	HV
	CM1	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}$ >0.5, p<0.05	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM2	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12} = 0.5, p = 1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM3	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> >0.5, p<0.05	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM4	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
P1	CM5	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM6	$\hat{A}_{12} < 0.1$ , p<0.05	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM7	$\hat{A}_{12} < 0.1$ , p<0.05	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}$ >0.5, p<0.05	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM8	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}$ >0.5, p<0.05	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM9	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> >0.5, p<0.05	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM1	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM2	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
P2	CM3	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}=0.5, p=1.0$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM4	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM5	$\hat{A}_{12} < 0.1$ , p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM6	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM7	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM8	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM9	$\hat{A}_{12} < 0.1$ , p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM1	$\hat{A}_{12} < 0.1$ , p<0.05	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM2	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM3	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM4	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
P3	CM5	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM6	$\hat{A}_{12} < 0.1$ , p<0.05	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM7	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM8	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM9	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ <0.1, p<0.05	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM1	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM2	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM3	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM4	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
P4	CM5	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM6	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM7	$\hat{A}_{12} < 0.1, p < 0.05$	Â <sub>12</sub> =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM8	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05
	CM9	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ =0.5, p= <b>1.0</b>	$\hat{A}_{12}=0.5, p=1.0$	$\hat{A}_{12} < 0.1, p < 0.05$	$\hat{A}_{12}$ >0.9, p<0.05

# Appendix B. Statistic Analysis Result for RQ2

			01	0	2 <sub>P1</sub>	(	)3	OF	VP2	HV	
СМі	СМј	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р
	CM2	0.32	< 0.05	0.34	< 0.05	0.50	< 0.05	0.33	< 0.05	0.67	< 0.05
	CM3	0.34	< 0.05	0.33	< 0.05	0.50	0.56	0.34	< 0.05	0.65	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.50	1.0	0	< 0.05	1	< 0.05
CM1	CM5	0	< 0.05	0	< 0.05	0.50	< 0.05	0	< 0.05	1	< 0.05
CM1	CM6	0	< 0.05	0	< 0.05	0.50	< 0.05	0	< 0.05	1	< 0.05
	CM7	0.91	< 0.05	0.95	< 0.05	0.43	< 0.05	0.81	< 0.05	0.04	< 0.05
	CM8	0.92	< 0.05	0.96	< 0.05	0.46	< 0.05	0.87	< 0.05	0.04	< 0.05
	CM9	0.90	< 0.05	0.95	< 0.05	0.43	< 0.05	0.80	< 0.05	0.05	< 0.05
	CM3	0.53	< 0.05	0.49	< 0.05	0.50	< 0.05	0.53	< 0.05	0.48	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.50	1.0	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0	< 0.05	0.50	1.0	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0	< 0.05	0.50	1.0	0	< 0.05	1	< 0.05
	CM7	0.99	< 0.05	0.99	< 0.05	0.43	< 0.05	0.92	< 0.05	0.01	< 0.05
	CM8	0.99	< 0.05	1.00	< 0.05	0.46	< 0.05	0.96	< 0.05	0.01	< 0.05
	CM9	0.99	< 0.05	1.00	< 0.05	0.43	< 0.05	0.93	< 0.05	0.01	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.51	< 0.05	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0	< 0.05	0.50	< 0.05	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0	< 0.05	0.50	< 0.05	0	< 0.05	1	< 0.05
CIVIS	CM7	0.94	< 0.05	0.96	< 0.05	0.44	< 0.05	0.86	< 0.05	0.01	< 0.05
	CM8	0.95	< 0.05	0.97	< 0.05	0.47	< 0.05	0.91	< 0.05	0.01	< 0.05
	CM9	0.94	< 0.05	0.97	< 0.05	0.44	< 0.05	0.86	< 0.05	0.01	< 0.05
	CM5	0.22	< 0.05	0.08	< 0.05	0.5	1.0	0.20	< 0.05	0.80	< 0.05
	CM6	0.10	< 0.05	0.09	< 0.05	0.5	1.0	0.09	< 0.05	0.84	< 0.05
CM4	CM7	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
	CM8	1	< 0.05	1	< 0.05	0.46	< 0.05	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
	CM6	0.47	< 0.05	0.47	< 0.05	0.5	1.0	0.47	< 0.05	0.55	< 0.05
CM5	CM7	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
CM5	CM8	1	< 0.05	1	< 0.05	0.46	< 0.05	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
	CM7	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
CM6	CM8	1	< 0.05	1	< 0.05	0.46	< 0.05	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.43	< 0.05	1	< 0.05	0	< 0.05
CM7	CM8	0.45	< 0.05	0.48	< 0.05	0.52	< 0.05	0.47	< 0.05	0.57	< 0.05
CIVI7	CM9	0.45	< 0.05	0.42	< 0.05	0.51	0.11	0.46	< 0.05	0.56	< 0.05
CM8	CM9	0.49	< 0.05	0.42	< 0.05	0.48	< 0.05	0.47	< 0.05	0.50	< 0.05

# Table B 1. Mann-Whitney U Test between CMi VS CMj of NSGA-II For P1 with Bandy

<b>67 6</b>	<b>67 6</b>	(	D1	0	2 <sub>P2</sub>	(	)3	OF	VP2	Н	V
CMi	СМј	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р
	CM2	0.16	< 0.05	0.5	1.0	0.5	1.0	0.16	< 0.05	0.83	< 0.05
	CM3	0.17	< 0.05	0.5	1.0	0.5	1.0	0.17	< 0.05	0.81	< 0.05
	CM4	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
<b>C</b> ) (1	CM5	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
CM1	CM6	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1.00	< 0.05	0.01	< 0.05
	CM8	0.99	< 0.05	0.5	1.0	0.5	1.0	0.99	< 0.05	0.01	< 0.05
	CM9	1.00	< 0.05	0.5	1.0	0.5	1.0	1.00	< 0.05	0.01	< 0.05
	CM3	0.51	< 0.05	0.5	1.0	0.5	1.0	0.51	< 0.05	0.49	0.59
	CM4	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM8	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM4	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	1	< 0.05
CMS	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0.00	< 0.05
	CM8	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0.00	< 0.05
CM3	CM9	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0.00	< 0.05
	CM5	0	< 0.05	0.5	1.0	0.5	1.0	0	< 0.05	0.99	< 0.05
	CM6	0.03	< 0.05	0.5	1.0	0.5	1.0	0.03	< 0.05	0.99	< 0.05
CM4	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM8	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM6	0.54	< 0.05	0.5	1.0	0.5	1.0	0.54	< 0.05	0.48	0.69
CM5	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
CIVIS	CM8	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
	CM7	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
CM6	CM8	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
CM6	CM9	1	< 0.05	0.5	1.0	0.5	1.0	1	< 0.05	0	< 0.05
CM7	CM8	0.52	< 0.05	0.5	1.0	0.5	1.0	0.52	0.8647942	0.48	0.52
	CM9	0.25	< 0.05	0.5	1.0	0.5	1.0	0.25	< 0.05	0.52	0.36
CM8	CM9	0.25	< 0.05	0.5	1.0	0.5	1.0	0.25	< 0.05	0.53	0.17

Table B 2. Mann-Whitney U Test between CMi VS CMj of NSGA-II For P2 with Bandy

(T) (T)	01.61		01	0	2 <sub>P3</sub>	(	)3	O	FV <sub>P3</sub>	J	IV
CMi	СМј	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р
	CM2	0.18	< 0.05	0.18	< 0.05	0.5	1	0.18	< 0.05	0.86	< 0.05
	CM3	0.13	< 0.05	0.14	< 0.05	0.5	1	0.13	< 0.05	0.83	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
CM1	CM5	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
	CM6	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
	CM7	0.93	< 0.05	0.93	< 0.05	0.5	1	0.94	< 0.05	0.01	< 0.05
	CM8	0.95	< 0.05	0.95	< 0.05	0.5	1	0.95	< 0.05	0.02	< 0.05
	CM9	0.97	< 0.05	0.97	< 0.05	0.5	1	0.97	< 0.05	0.01	< 0.05
	CM3	0.58	< 0.05	0.59	< 0.05	0.5	1	0.59	< 0.05	0.42	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
	CM7	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM8	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM4	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
<b>CN 12</b>	CM6	0	< 0.05	0	< 0.05	0.5	1	0	< 0.05	1	< 0.05
CM3	CM7	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM8	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0.00	< 0.05
	CM5	0.04	< 0.05	0.05	< 0.05	0.5	1	0.03	< 0.05	0.96	< 0.05
	CM6	0.01	< 0.05	0.05	< 0.05	0.5	1	0	< 0.05	0.94	< 0.05
CM4	CM7	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
	CM8	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
	CM6	0.56	< 0.05	0.55	< 0.05	0.5	1	0.56	< 0.05	0.44	< 0.05
C) (5	CM7	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
CM5	CM8	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
	CM7	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
CM6	CM8	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
Cino	CM9	1	< 0.05	1	< 0.05	0.5	1	1	< 0.05	0	< 0.05
CM7	CM8	0.50	0.7988288	0.51	0.7567437	0.5	1	0.51	0.8076762	0.53	0.05
CM/	CM9	0.48	0.5942967	0.46	0.2079487	0.5	1	0.47	0.4204473	0.49	0.33
CM8	CM9	0.48	0.714988	0.45	1.88E-01	0.5	1	0.47	0.5305118	0.45	0.16

Table B 3. Mann-Whitney U Test between CMi VS CMj of NSGA-II For P3 with Bandy

CMi	CD CI		01	(	02 <sub>P4</sub>		03	0	FV <sub>P4</sub>	Н	V
СМі	СМј	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р	$\widehat{A}_{12}$	Р
	CM2	0.13	< 0.05	0.5	1	0.5	1	0.13	< 0.05	0.81	< 0.05
	CM3	0.14	< 0.05	0.5	1	0.5	1	0.14	< 0.05	0.84	< 0.05
	CM4	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
CMI	CM5	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
CM1	CM6	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
	CM7	0.90	< 0.05	0.5	1	0.5	1	0.90	< 0.05	0.01	< 0.05
	CM8	0.92	< 0.05	0.5	1	0.5	1	0.92	< 0.05	0.01	< 0.05
	CM9	0.92	< 0.05	0.5	1	0.5	1	0.92	< 0.05	0.01	< 0.05
	CM3	0.47	< 0.05	0.5	1	0.5	1	0.47	< 0.05	0.53	< 0.05
	CM4	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
CM2	CM6	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
	CM7	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0.00	< 0.05
	CM8	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0.00	< 0.05
	CM9	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0.00	< 0.05
	CM4	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
	CM5	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
<b>C</b> 1 (2)	CM6	0	< 0.05	0.5	1	0.5	1	0	< 0.05	1	< 0.05
CM3	CM7	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0.00	< 0.05
	CM8	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
CM3	CM9	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0.00	< 0.05
	CM5	0	< 0.05	0.5	1	0.5	1	0	< 0.05	0.99	< 0.05
	CM6	0	< 0.05	0.5	1	0.5	1	0	< 0.05	0.99	< 0.05
CM4	CM7	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM8	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM6	0.50	< 0.05	0.5	1	0.5	1	0.50	< 0.05	0.48	< 0.05
C) 15	CM7	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
CM5	CM8	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM7	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
CM6	CM8	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
	CM9	1	< 0.05	0.5	1	0.5	1	1	< 0.05	0	< 0.05
0.45	CM8	0.40	< 0.05	0.5	1	0.5	1	0.40	< 0.05	0.51	0.72
CM/	CM9	0.59	< 0.05	0.5	1	0.5	1	0.59	< 0.05	0.49	0.18
CM8	CM9	0.61	< 0.05	0.5	1	0.5	1	0.61	< 0.05	0.49	0.27

# Table B 4. Mann-Whitney U Test between CMi VS CMj of NSGA-II For P4 with Bandy

# Appendix C. Statistic Analysis Result for RQ3

Metrics		Nparm	DF	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>
	C	2	2	1.0209943	0.122614007	854135.787	<.0001
01	М	2	2	0.001987	0.122614007	1662.2497	<.0001
01	C*M	4	4	0.0010111	0.122614006	422.9395	<.0001
	Residuals	53878	8	0.0322016	0.000001		
02	С	2	2	0.15183762	0.002087073	2748.4736	<.0001
	М	2	2	0.0081096	0.002087073	146.7951	<.0001
$O_{2P1}$	C*M	4	4	0.00916384	0.002087078	82.9391	<.0001
	Residuals	53878	8	1.4882274	0.000028		
	С	2	2	0.15183762	0.002087073	2748.4736	<.0001
02	М	2	2	0.0081096	0.002087073	146.7951	<.0001
03	C*M	4	4	0.00916384	0.002087078	82.9391	<.0001
	Residuals	53878	8	1.4882274	0.000028		
	С	2	2	31.391177	0.141840513	672500.1677	<.0001
OEV	М	2	2	0.046888	0.141840513	1004.4985	<.0001
OFV	C*M	4	4	0.02388	0.141840513	255.7978	<.0001
	Residuals	53878	8	1.257467	0.00002		
	С	2	2	18.945114	0.620483997	80858.1169	<.0001
шу	М	2	2	0.039624	0.620483993	169.115	<.0001
пу	C*M	4	4	0.013086	0.620483994	27.9257	<.0001
	Residuals	3291	8	0.385542	0.00012		

Table C 2. Two-Way Analysis of Variance For P2 with Bandy

Metrics		Nparm	DF	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>
	С	2	2	156.71749	0.216848307	389146.2158	<.0001
01	М	2	2	0.39688	0.216848307	985.4949	<.0001
01	C*M	4	4	0.13842	4.86671362	171.858	<.0001
	Residuals	42714	8	8.60092	0.0002		
O2 <sub>P2</sub>	С	2	2	0	0	-	-
	М	2	2	0	0	-	-
	C*M	4	4	0	0	-	-
	Residuals	42714	8	0	0		
	С	2	2	0	0	-	-
02	М	2	2	0	0	-	-
03	C*M	4	4	0	0	-	-
	Residuals	44234	8	0	0		
	С	2	2	17.413055	0.072282767	389146.2157	<.0001
OEV	М	2	2	0.044098	0.07228277	985.4949	<.0001
OFV	C*M	4	4	0.01538	0.07228277	171.858	<.0001
	Residuals	42714	8	0.955658	0.00002		
	С	2	2	40.464022	0.784402877	124657.9089	<.0001
1137	М	2	2	0.197719	0.784402877	609.1143	<.0001
HV	C*M	4	4	0.116942	0.784402878	180.1321	<.0001
	Residuals	3291	8	0.53413	0.00016		

Metrics		Nparm	DF	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F</b> )
01	С	2	2	153.68297	0.241220187	406804.858	<.0001
	М	2	2	0.26054	0.241220187	689.6525	<.0001
	C*M	4	4	0.10385	0.24122019	137.4496	<.0001
	Residuals	41338	8	7.80835	0.0002		
O2 <sub>P3</sub>	С	2	2	5.2681164	0.88310765	182550.0372	<.0001
	М	2	2	0.0111276	0.88310765	385.5915	<.0001
	C*M	4	4	0.0229758	0.88310765	398.077	<.0001
	Residuals	41338	8	0.596476	0.00001		
O3	С	2	2	0	0	-	-
	М	2	2	0	0	-	-
	C*M	4	4	0	0	-	-
	Residuals	44234	8	0	0		
OFV	С	2	2	23.913254	0.37477595	389146.2157	<.0001
	М	2	2	0.042147	0.374775947	985.4949	<.0001
	C*M	4	4	0.020896	0.374775947	171.858	<.0001
	Residuals	41338	8	1.35219	0.00003		
HV	С	2	2	2.6124636	0.091279173	38898.9544	<.0001
	М	2	2	0.0123362	0.09127917	183.6837	<.0001
	C*M	4	4	0.0083831	0.091279173	62.4113	<.0001
	Residuals	3291	8	0.1105122	0.000034		

Table C 3. Two-Way Analysis of Variance For P3 with Bandy

Table C 4. Two-Way Analysis of Variance For P4 with Bandy

Metrics		Nparm	DF	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>
01	С	2	2	143.27413	0.217201457	339324.3271	<.0001
	М	2	2	0.4433	0.21720146	1049.8926	<.0001
	C*M	4	4	0.16871	0.217201458	199.7823	<.0001
	Residuals	44234	8	9.33854	0.0002		
O2 <sub>P4</sub>	С	2	2	0	0	-	-
	М	2	2	0	0	-	-
	C*M	4	4	0	0	-	-
	Residuals	44234	8	0	0		
O3	С	2	2	0	0	-	-
	М	2	2	0	0	-	-
	C*M	4	4	0	0	-	-
	Residuals	44234	8	0	0		
OFV	C	2	2	23.913254	0.37477595	389146.2157	<.0001
	М	2	2	0.042147	0.374775947	985.4949	<.0001
	C*M	4	4	0.020896	0.374775947	171.858	<.0001
	Residuals	41338	8	1.35219	0.00003		
HV	C	2	2	40.781037	0.784292033	120817.7814	<.0001
	М	2	2	0.215505	0.784292033	638.4545	<.0001
	C*M	4	4	0.132244	0.784292034	195.8929	<.0001
	Residuals	3291	8	0.555425	0.00017		